

# EHD-Net: A Hybrid Approach to Brain Tumor Segmentation in MRI Using U-Net Transformer Architecture with Double Attention

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Accurate segmentation of brain tumors from magnetic resonance imaging (MRI) plays a crucial role in diagnosis, treatment planning, and follow-up. EHD-Net (Efficient Hybrid Double-Attention Network) is proposed as a hybrid architecture that combines the strengths of convolutional and Transformer-based approaches while maintaining computational efficiency. The model employs an optimized U-Net backbone with depth wise separable convolutions to reduce parameters, a 3D Contextual Transformer (CoT) at the bottleneck to capture long-range dependencies, and lightweight Double Attention (DA) modules in skip connections to refine local boundaries. Trained and evaluated on the BraTS 2021 dataset with multimodal MRI sequences (T1, T1ce, T2, FLAIR), EHD-Net achieves state-of-the-art performance with an average Dice Similarity Coefficient (DSC) of 93.2 % (95.1 % WT, 92.4 % TC, 92.0 % ET), IoU of 85.1 %, HD<sub>95</sub> of 5.5 mm, and MSD of 1.2 mm. Importantly, EHD-Net delivers the fastest inference among the compared models, with an average processing time of 9 seconds per MRI volume, making it suitable for near real-time clinical deployment. These results highlight EHD-Net as an effective, robust, and efficient solution for brain tumor segmentation in multimodal MRI, bridging the gap between high accuracy and practical usability in clinical workflows.

**Keywords:** Brain tumor segmentation, Multimodal MRI, U-Net, Transformer, Double attention, Hybrid deep learning, BraTS dataset

## 1 Introduction

Brain tumors, particularly gliomas, are among the most aggressive malignancies of the central nervous system, with high morbidity and mortality rates, making timely diagnosis and precise treatment planning essential for improving patient outcomes<sup>1</sup>. Accurate delineation of tumor subregions whole tumor (WT), tumor core (TC), and enhancing tumor (ET) is a critical prerequisite for surgical resection, radiotherapy planning, and longitudinal monitoring<sup>2</sup>. Among available imaging modalities, Magnetic Resonance Imaging (MRI) remains the gold standard for brain tumor analysis due to its superior soft-tissue contrast, non-invasiveness, and multimodal acquisition capability<sup>3</sup>. MRI sequences such as T1, T1ce, T2, and FLAIR provide complementary perspectives by highlighting structural, vascular, and pathological features of tumors<sup>4</sup>. However, manual segmentation of tumor subregions by radiologists is highly time-consuming, subject to inter-observer variability, and impractical in large-scale clinical workflows<sup>5</sup>. In recent years, artificial intelligence (AI) has played an increasingly important role in

healthcare by enabling data driven disease diagnosis, prognosis, and decision support. AI based models have demonstrated strong potential in improving diagnostic accuracy and reducing inter-observer variability across a wide range of clinical applications, including cardiovascular disease prediction, oncology, and medical imaging. In particular, the ability of deep learning models to extract complex patterns from high-dimensional clinical and imaging data has significantly enhanced disease characterization and risk stratification. These advances highlight the broader relevance of AI-driven approaches in medical decision-making and provide important context for the application of deep learning techniques to brain tumor segmentation from MRI, where accurate and efficient delineation of pathological regions is critical for diagnosis, treatment planning, and follow up.

Over the past decade, deep learning has emerged as the dominant paradigm for automated brain tumor segmentation. Early convolutional neural network (CNN)-based approaches, such as patch-wise and voxel-based methods, achieved moderate accuracy improvements over classical machine learning but were constrained by limited receptive fields and

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inability to capture long-range spatial dependencies<sup>6,7</sup>. A major breakthrough came with U-Net<sup>8</sup>, whose encoder-decoder architecture with skip connections enabled fine localization and robust feature fusion. This architecture inspired numerous variants, including 3D U-Net, Attention U-Net, Residual U-Net, and Dense U-Net, which have consistently performed well in BraTS challenges and other medical benchmarks<sup>9</sup>. Despite these successes, conventional U-Net variants struggle with irregular tumor morphologies, heterogeneous textures, and fuzzy boundaries, as their convolutional kernels primarily capture local features. Recently, Transformer-based architectures have been adapted from natural language processing to computer vision and medical imaging tasks. Their self-attention mechanisms allow modeling of global dependencies across entire feature maps, making them highly effective for complex tumor structures<sup>10</sup>. Hybrid architectures, such as TransUNet and UNETR, integrate CNN backbones with transformer encoders, achieving state-of-the-art accuracy by leveraging both local and global context<sup>11</sup>. However, these approaches are computationally expensive and heavily data-dependent, which limits their applicability in resource-constrained clinical environments.

Parallel to this, attention mechanisms have been integrated within U-Net variants to enhance feature selection. Attention gates, channel-spatial attention modules, and residual attention schemes have been shown to suppress irrelevant regions while emphasizing tumor-relevant structures<sup>12</sup>. Nevertheless, single-stage attention often falls short in balancing global and local feature representation. To address this, Double Attention (DA) has been proposed<sup>13,14</sup>, which operates in two steps: (i) global feature aggregation across spatial dimensions, followed by (ii) adaptive redistribution to local tumor subregions. This dual mechanism enhances both contextual understanding and boundary refinement, which is particularly crucial for accurate segmentation of gliomas with diffuse or irregular borders.

Existing CNN-based approaches suffer from limited receptive fields, Transformer-based methods impose high computational costs, and standard U-Net attention mechanisms inadequately balance global context with fine boundary precision. These challenges highlight the need for a model that is accurate, efficient, and robust, while remaining feasible for clinical deployment.

In this study, EHD-Net (Efficient Hybrid Double-Attention Network), a novel deep learning framework

for brain tumor segmentation in MRI, is proposed. The key contributions of this work are:

- i. Efficient U-Net Backbone: An optimized encoder-decoder architecture designed with reduced parameters and faster inference while retaining segmentation accuracy.
- ii. 3D Contextual Transformer (CoT): A volumetric Transformer block integrated at the bottleneck to capture long-range dependencies across multimodal MRI data.
- iii. Lightweight Double Attention (DA): Attention modules embedded in skip connections to enhance global context while simultaneously refining local tumor boundaries.

By combining efficiency, contextual modeling, and fine boundary refinement, EHD-Net addresses the shortcomings of prior methods. Extensive experiments on the BraTS 2021 dataset demonstrate that EHD-Net achieves superior accuracy, robustness, and computational efficiency, making it a practical candidate for near-real-time clinical workflows.

## 2 Literature Work

Automated brain tumor segmentation has attracted significant attention over the past decade, driven by advances in deep learning and the availability of large annotated datasets such as the Brain Tumor Segmentation (BraTS) challenges. These competitions have provided standardized benchmarks, enabling fair evaluation of algorithms and driving rapid progress in the field. Research efforts have evolved from early convolutional neural network (CNN) designs to U-Net variants, Transformer-based approaches, and more recently, hybrid architectures that integrate both convolutional and attention mechanisms.

Table 1 summarizes representative state-of-the-art models for brain tumor segmentation. Early CNN-based approaches such as patch-wise CNNs<sup>15</sup> and 3D U-Net<sup>16,17</sup> established the foundation but were limited by local receptive fields and irregular boundary delineation. Variants including Attention U-Net and Residual U-Net<sup>18,19</sup> improved feature selection and gradient flow, while Dense U-Net<sup>20</sup> enhanced feature reuse, though often at the cost of increased memory demands. Transformer-based methods such as TransUNet<sup>21</sup>, UNETR<sup>10</sup>, and Swin-UNet<sup>22</sup> effectively capture long-range dependencies and global context but typically require extensive computational resources and large annotated datasets. Hybrid architectures integrating contextual transformers and multi-attention modules<sup>23,24</sup> demonstrated improved

Table 1 — Representative state-of-the-art models for brain tumor segmentation

Model	Architecture Type	Dataset	Remarks
CNN (Patchbased) <sup>15</sup>	Deep CNN	BraTS 2018	Early deep learning approach; simple design but limited global context and boundary precision
3D U-Net <sup>16, 17</sup>	encoder-decoder	BraTS 2019	Strong volumetric representation and skip connections; struggles with irregular tumor boundaries
Attention U-Net <sup>18</sup>	U-Net + Attention Gates	BraTS 2019	Enhances feature selection and suppresses irrelevant regions; computationally heavier than vanilla U-Net
Residual U-Net <sup>19</sup>	U-Net + Residual Connections	BraTS 2019	Better gradient flow for deeper networks; still limited in capturing global dependencies
Dense U-Net <sup>20</sup>	U-Net + Dense Connections	BraTS 2020	Improves feature reuse and generalization; higher memory requirements
TransUNet <sup>21</sup>	U-Net + Transformer	BraTS 2020	Captures long-range dependencies; requires large datasets and higher computation
UNETR <sup>10</sup>	Transformer Encoder + CNN Decoder	BraTS 2021	Achieves high accuracy with global context modeling; very heavy in computation and memory
Swin-UNet <sup>22</sup>	U-Net + Swin Transformer	BraTS 2021	Hierarchical representation learning improves efficiency; still relatively complex compared to CNN-based models
Double Attention U-Net <sup>23</sup>	U-Net + Double Attention	BraTS 2021	Enhances both global and local features; higher complexity than singleattention U-Nets
Hybrid CoTDA U-Net <sup>24</sup>	U-Net + Contextual Transformer + Double Attention	BraTS 2020	Better boundary delineation; increased architectural complexity
Efficient U-Net <sup>25</sup>	Optimized U-Net	BraTS 2021	Reduced complexity with depthwise separable convolutions; maintains competitive accuracy

boundary precision, though with added architectural complexity. Efficient U-Net designs<sup>25</sup> focused on reducing computational overhead while preserving segmentation quality, making them more suitable for deployment on limited hardware.

Beyond architectural innovations, another emerging challenge is handling the multi-modality of MRI scans. Most methods rely on four sequences (T1, T1ce, T2, FLAIR), yet balancing their complementary information while remaining robust to missing modalities remains a difficult task. Furthermore, many of the existing approaches are optimized for benchmark datasets and often underperform in real-world scenarios where imaging quality, scanner variability, and tumor heterogeneity differ from controlled experimental conditions. Clinical adoption is further hindered by high inference latency of transformer-heavy models and the lack of interpretability in deep networks, which limits trust from practitioners.

### 3 Methods and Materials

#### 3.1 Datasets and Preprocessing

The performance of deep learning models for brain tumor segmentation depends critically on the availability of high-quality annotated datasets. This work relies primarily on the Brain Tumor Segmentation (BraTS) challenge dataset, which provides multimodal MRI scans along with expert

annotated ground truth masks for tumor sub-regions. Other datasets such as TCGA-TCIA, REMBRANDT, and Figshare collections exist and are often used for pretraining or cross validation, but in this study, the focus is on the BraTS for training and evaluation of the proposed EHD-Net model.

##### 3.1.1 BraTS Dataset

The Brain Tumor Segmentation (BraTS) challenge series (2012–2021) has become the de facto benchmark for brain tumor segmentation research<sup>26,27</sup>. Each BraTS dataset provides multimodal MRI scans of glioma patients, including T1-weighted, contrast-enhanced T1 (T1ce), T2-weighted, and FLAIR modalities. Tumor regions are annotated by expert neuroradiologists, with labels covering the whole tumor (WT), tumor core (TC), and enhancing tumor (ET). BraTS datasets contain both lowgrade glioma (LGG) and high-grade glioma (HGG) cases, ensuring diversity in tumor presentation. Evaluation metrics typically include Dice Similarity Coefficient (DSC), Hausdorff Distance (HD), and Intersection over Union (IoU).

The BraTS dataset provides four complementary MRI modalities, each capturing different tumor characteristics as shown in Fig. 1. T1-weighted images offer high anatomical detail but limited visibility of tumor boundaries. Contrast enhanced T1

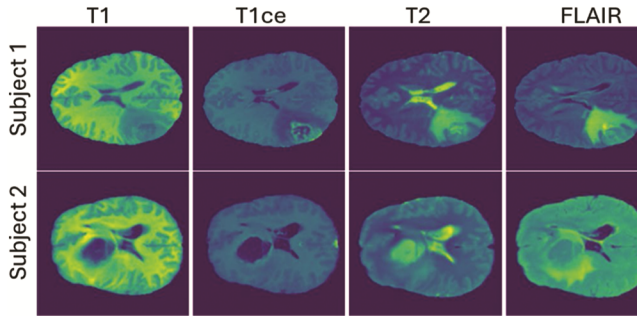


Fig. 1 — Illustration of T1, T1ce, T2, and FLAIR modalities from the BraTS dataset, highlighting their complementary tumor representations

(T1ce) highlights the enhancing tumor (ET) region, making it easier to differentiate active tumor tissue from surrounding structures. T2-weighted images are particularly sensitive to edema and fluid accumulation, thereby revealing peritumoral changes. FLAIR imaging suppresses the cerebrospinal fluid (CSF) signal, which enhances the visibility of hyperintensities associated with tumor-related abnormalities. When these modalities are fused, they provide a comprehensive representation of the tumor, enabling accurate identification of the whole tumor (WT), tumor core (TC), and enhancing tumor (ET) sub-regions<sup>28</sup>. This multimodal integration is essential for achieving robust performance in deep learning models such as the proposed EHD-Net.

### 3.1.2 Preprocessing Pipeline

To prepare the MRI scans for training, a standardized preprocessing pipeline is applied to ensure consistency and robustness across patients and scanners. First, skull stripping is performed to remove non-brain tissues, ensuring that the analysis focuses exclusively on relevant regions. Next, the MRI volumes are resampled to a uniform voxel spacing, typically  $1 \times 1 \times 1 \text{ mm}^3$ , to standardize spatial resolution. Intensity normalization is then applied, using z-score normalization to reduce variability in intensity values across different scans<sup>29</sup>. To handle memory constraints while preserving volumetric context, 3D patches of fixed size  $128 \times 128 \times 128$  are extracted from the resampled volumes, which serve as the input to the proposed EHD-Net. At last, data augmentation techniques such as rotation, flipping, elastic deformation, and Gaussian noise injection are employed to increase dataset diversity and improve model generalization. This preprocessing ensures that the input to EHD-Net is harmonized and suitable for robust training and evaluation.

## 4 Proposed EHD-Net (EFFICIENT U-Net+COT+DA) Model

In this section, the proposed EHD-Net (Efficient Hybrid Double-Attention Network), designed to achieve accurate and efficient brain tumor segmentation from multimodal MRI scans. The proposed EHD-Net is a three-dimensional encoder decoder network designed for efficient and accurate brain tumor segmentation from multimodal MRI volumes. The architecture combines an optimized U-Net backbone with a 3D Contextual Transformer module and lightweight attention mechanisms. The backbone of EHD-Net is based on an Efficient U-Net encoder decoder structure, which is optimized to reduce the number of trainable parameters while preserving representational capacity. To enhance global context modeling, a 3D Contextual Transformer (CoT) module is integrated at the bottleneck stage of the network. Lightweight Double Attention (DA) modules are introduced in the skip connections between encoder and decoder paths, enabling the model to simultaneously capture global dependencies and refine local tumor boundaries. The overall design emphasizes computational efficiency while preserving the ability to model both global contextual dependencies and fine grained boundary information.

i Efficient U-Net Backbone: The backbone of EHD-Net follows a standard 3D U-Net topology consisting of an encoder path, a bottleneck, and a symmetric decoder path. To reduce computational cost and memory usage, two architectural optimizations are consistently applied throughout the network: reduced channel widths and depthwise separable convolutions. The encoder comprises four resolution levels. At each level, two consecutive convolutional blocks are followed by downsampling via strided convolution. The number of feature channels across the encoder stages is set to 32, 64, 128, and 256, respectively, which is lower than that of conventional 3D U-Net architectures. This design choice limits parameter growth while retaining sufficient representational capacity for multimodal MRI features. Each convolutional block employs a 3D depthwise separable convolution, decomposed into a depthwise convolution and a subsequent  $1 \times 1 \times 1$  pointwise convolution. Batch normalization and ReLU activation are applied after the pointwise convolution. This configuration significantly reduces the number of trainable parameters and floating-point operations compared to standard 3D convolutions. The decoder mirrors the

encoder structure with four upsampling stages. Feature map resolution is restored using trilinear upsampling, followed by convolutional refinement. Decoder channel dimensions' decrease symmetrically as 256, 128, 64, and 32. Skip connections are introduced between corresponding encoder and decoder stages to preserve spatial detail and facilitate gradient flow. In the proposed EHD-Net, architectural efficiency is achieved by systematically replacing all standard 3D convolutional layers in both the encoder and decoder paths with 3D depthwise separable convolutions.

Specifically, each convolutional block is decomposed into a depthwise 3D convolution, which operates independently on each input channel, followed by a  $1 \times 1 \times 1$  pointwise convolution to perform channel wise feature mixing. This replacement is applied consistently across all encoder blocks, bottleneck adjacent layers, and decoder refinement blocks, ensuring a uniform reduction in parameter count and computational complexity throughout the network. Besides convolutional factorization, EHD-Net employs reduced channel widths compared to a conventional 3D U-Net. While a standard 3D U-Net typically uses channel dimensions of 64, 128, 256, 512 across successive encoder stages, the proposed architecture adopts a reduced configuration of 32, 64, 128, 256, resulting in an approximate 50 % reduction in channel capacity at each resolution level. The decoder mirrors this configuration symmetrically. This deliberate reduction significantly lowers memory usage and floating-point operations while preserving sufficient representational capacity for multimodal MRI features. The combined use of depthwise separable convolutions and reduced channel widths enables EHD-Net to maintain competitive segmentation accuracy with substantially lower computational overhead, thereby supporting its suitability for efficient volumetric inference in clinical settings.

ii 3D Contextual Transformer (CoT): While CNNs are effective at local feature extraction, they have limited capacity for modeling long range dependencies. To address this, a 3D Contextual Transformer (CoT) is incorporated at the bottleneck of EHD-Net. The CoT block applies self-attention across volumetric patches, capturing relationships between distant tumor regions<sup>30</sup>. This enables the model to integrate global context across multimodal MRI scans, which is particularly beneficial for segmenting irregularly shaped tumors and diffuse boundaries. The internal operation of the CoT block is illustrated in Fig. 2.

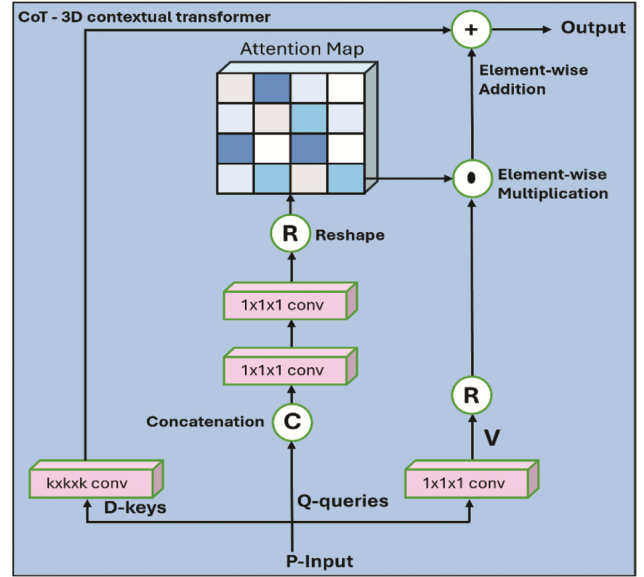


Fig. 2 — 3D contextual transformer (CoT) block for brain tumor segmentation from MRI images in the proposed EHDNet

The CoT block extends the standard self-attention mechanism by incorporating both static and dynamic contextual information into the feature learning process. Given a 3D input feature map  $P = \mathbb{R}^{H \times W \times C \times K}$  with dimensions (H, W, C) and K channels, the block first transforms P into queries Q, keys D, and values V using learnable embedding matrices  $W_Q$ ,  $W_D$ , and  $W_V$ .

To enrich the representation of each key with local structural information, a  $k \times k \times k$  convolution is applied over the keys, producing contextualized keys  $D^1 = \mathbb{R}^{H \times W \times C \times K}$ <sup>23</sup>. This convolution captures static contextual information by aggregating relationships among local neighboring keys. Subsequently, the contextualized keys D1 are combined with the queries Q to form an intermediate attention representation A, which can be formulated as:

$$A = [D^1, Q]W_\theta W_\delta \quad \dots (1)$$

where  $W_\theta$  and  $W_\delta$  are learnable parameters. The dynamic context is then introduced by performing element wise multiplication between the values V and the attention representation A, producing a new representation D2, which can be formulated as:

$$D^2 = V * A \quad \dots (2)$$

The output of the CoT block, denoted as Y, is obtained by merging the static context with  $D^1$  the dynamic context  $D^2$ , which can be formulated as:

$$Y = D^1 + D^2 \quad \dots (3)$$

This design allows the CoT block to simultaneously capture static local context (through convolutional aggregation) and dynamic global context (through attention-weighted interaction with values). Compared to conventional self-attention, CoT provides a richer and more discriminative representation of tumor features, making it particularly effective for complex volumetric MRI segmentation tasks.

To capture long-range spatial dependencies that cannot be effectively modeled by convolutional operations alone, a 3D Contextual Transformer (CoT) module is incorporated at the bottleneck of the network. At this stage, the feature maps are spatially compact but semantically rich, making it an appropriate location for global context modeling. The CoT module operates on the encoded feature tensor of size  $H/16 \times W/16 \times D/16 \times 256$ , and applies attention-based interactions to model relationships across distant spatial regions. By integrating both convolutional context aggregation and attention-based feature interaction, the CoT block enhances global representation without altering the dimensionality of the bottleneck features. The output of the CoT module is directly forwarded to the decoder. Restricting the transformer to the bottleneck stage minimizes computational overhead while allowing global contextual information to influence all subsequent decoding layers.

iii **Lightweight Double Attention Mechanism:** Accurate tumor segmentation requires balancing global representation with fine grained local details. To achieve this, Double Attention (DA) modules are embedded within the skip connections of EHD-Net<sup>31</sup>. The DA mechanism operates in two stages: (i) gathering global contextual features across the feature map, and (ii) redistributing them adaptively to refine local spatial regions<sup>32</sup>. Unlike heavy attention modules, our lightweight DA implementation is computationally efficient, making it suitable for real time clinical applications. By reinforcing skip connections with DA, EHD-Net enhances boundary precision while maintaining global consistency. The computational flow of the DA mechanism is depicted in Fig. 3.

Formally, given an input feature map  $P$ , the DA block first applies three  $1 \times 1 \times 1$  convolutional layers to generate three intermediate feature maps  $A$ ,  $U$ , and  $V$ . Here,  $A$  is used to capture the spatial attention map,  $U$  models the global dependencies, and  $V$  retains the

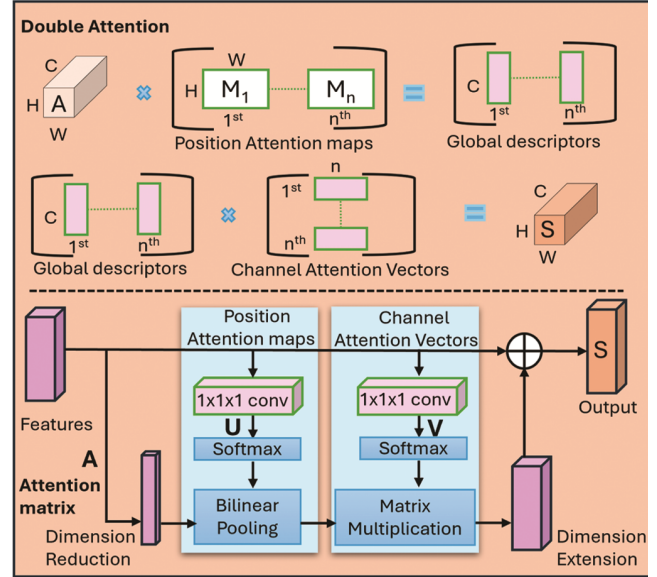


Fig. 3 — Double attention (DA) block for brain tumor segmentation from MRI images in the proposed EHDNet

original feature values. A softmax operation is applied to normalize the attention maps when required. The first attention step aggregates global features, while the second redistributes them to each spatial location, producing refined local representations  $s_i$  at position  $i$ . This two-stage mechanism ensures that both global and local contexts are considered simultaneously<sup>33</sup>. The final output  $S$  of the DA block can be expressed as:

$$S = \phi(P; W_\phi) [\text{softmax}(\theta(P; W_\theta))]^T \text{softmax}(\rho(P; W_\rho)) \quad \dots (4)$$

where  $W_\phi$ ,  $W_\theta$ , and  $W_\rho$  are learnable parameters. The operation involves two matrix multiplications that first gather global context features and then redistribute them adaptively to enhance local detail. Also, an additional  $1 \times 1 \times 1$  convolution encodes the refined output  $S$  back into the original feature space, followed by element-wise addition to  $P$ , thus enriching the representation without significantly increasing computational burden.

By attending to both spatial and channel-wise relationships, the DA block enables the network to selectively emphasize tumor-relevant features while suppressing irrelevant background. This dual mechanism strengthens the skip connections by preserving low-level details and aligning them with high level semantic context, leading to superior boundary delineation and overall segmentation performance.

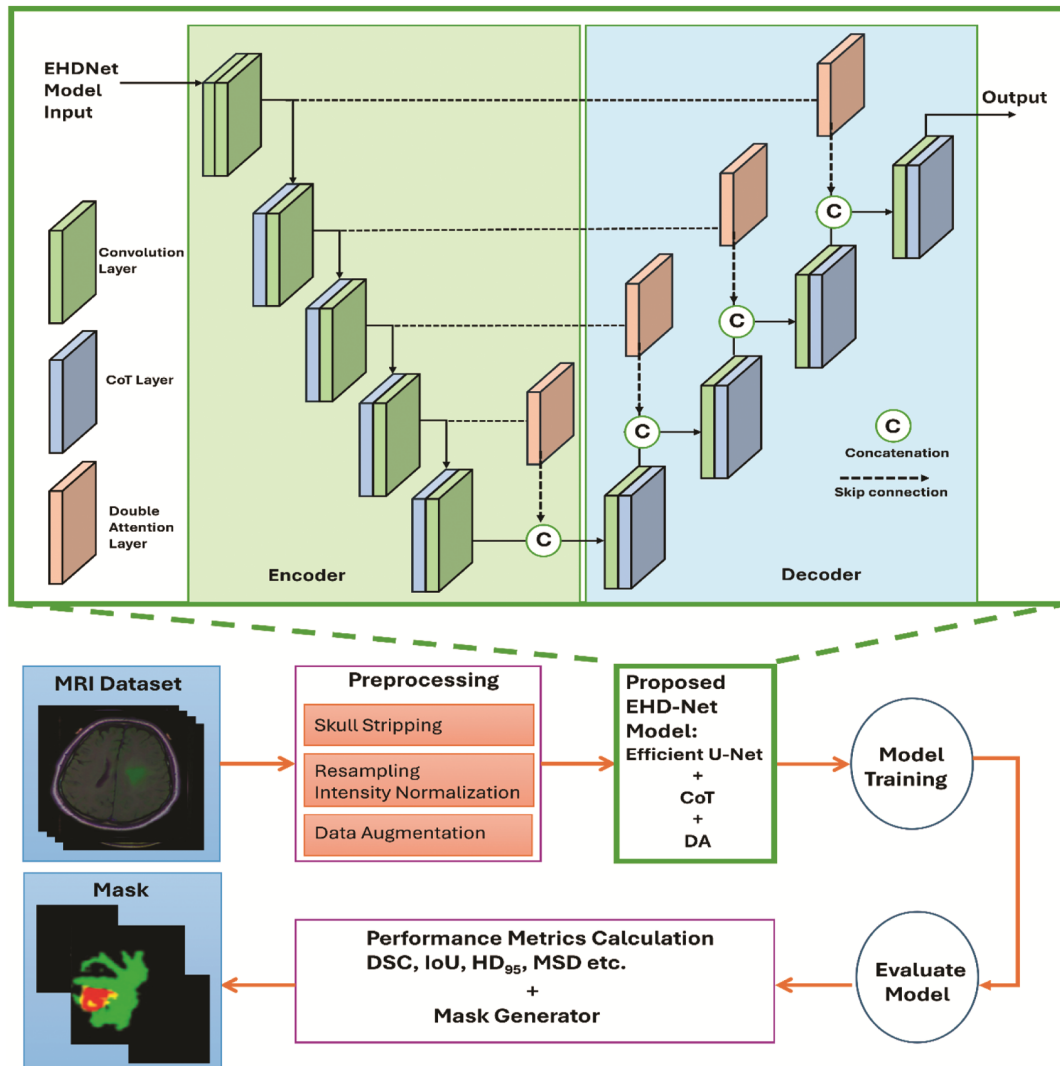


Fig. 4 — Overall architecture of the proposed EHD-Net, illustrating the Efficient U-Net backbone with reduced channel widths and depthwise separable convolutions, the 3D Contextual Transformer (CoT) at the bottleneck, and Double Attention (DA) modules integrated within skip connections

#### 4.1 Proposed EHD-Net

Conventional U-Net models become computationally expensive when extended to 3D volumetric data. To overcome this limitation, the proposed EHD-Net employs an optimized encoder decoder structure with depthwise separable convolutions and reduced channel widths, which substantially decreases the number of trainable parameters while preserving segmentation accuracy. The encoder progressively downsamples the input through strided convolutions, whereas the decoder reconstructs the segmentation mask via upsampling and skip connections.

To further enhance performance, EHD-Net integrates two novel modules within the encoder decoder pathway, as shown in Fig. 4. First, a 3D

Contextual Transformer (CoT) is inserted at the bottleneck to capture long-range spatial dependencies across MRI volumes. Second, lightweight Double Attention (DA) modules are embedded in the skip connections to simultaneously strengthen global feature representation and refine local tumor boundaries. Together, these modules enrich feature encoding and decoding, enabling more accurate volumetric segmentation of brain tumors.

For effective training, a composite segmentation loss combining Dice Loss and cross-entropy loss is adopted<sup>34</sup>. Dice Loss directly optimizes the overlap between predicted segmentation  $P$  and ground truth labels  $G$ , mitigating class imbalance, while cross entropy stabilizes voxel wise classification. Due to the

pronounced class imbalance present in the BraTS dataset, particularly for the enhancing tumor (ET) region a composite loss function combining Dice loss and cross entropy loss was employed. where  $\alpha$  controls the relative contribution of overlap based and voxel wise supervision. In this work, the weighting coefficient was empirically set to  $\alpha = 0.5$ , assigning equal importance to Dice and cross-entropy terms. This choice was found to provide stable convergence while effectively mitigating class imbalance, consistent with common practice in BraTS-related segmentation studies. Preliminary validation experiments confirmed that this balanced weighting achieved reliable performance across all tumor sub regions without requiring additional class specific weighting. The loss functions are defined as:

$$\mathcal{L}_{dice}(G, P) = 1 - \frac{2 \sum_{i=1}^I G_i^k P_i^k + \epsilon}{\sum_{i=1}^I (G_i^k)^2 + \sum_{i=1}^I (P_i^k)^2 + \epsilon} \quad \dots (5)$$

$$\mathcal{L}_{CE}(G, P) = - \sum_{k=1}^K \sum_{i=1}^I G_i^k \log P_i^k \quad \dots (6)$$

$$\mathcal{L}_{Seg}(G, P) = \alpha \mathcal{L}_{dice}(G, P) + (1 - \alpha) \mathcal{L}_{CE}(G, P) \quad \dots (7)$$

where  $I = H \times W \times C$  denotes the number of voxels,  $K$  is the number of classes  $\Omega_c = \{BG, NCR/NET, ED, ET\}$ ,  $G_i^k$  and  $P_i^k$  are the ground truth and predicted probabilities,  $\epsilon = 10^{-6}$  ensures numerical stability, and  $\alpha$  is a tunable weight. This hybrid loss ensures both accurate overlap optimization and stable convergence during training. In recapitulate, the proposed EHD-Net integrates its components as follows:

- An Efficient U-Net Backbone with reduced channel widths and depthwise separable convolutions across all convolutional layers.
- A 3D Contextual Transformer (CoT) module placed at the bottleneck to capture long range volumetric dependencies.
- Lightweight Double Attention (DA) modules embedded in skip connections to enhance boundary accuracy during feature fusion.

This structured integration enables EHD-Net to achieve a balance between segmentation accuracy, boundary precision, and computational efficiency. While Fig. 4 illustrates the high-level architecture, the above description specifies the exact placement and configuration of each component, ensuring methodological clarity and reproducibility. The complete workflow of the proposed framework begins with multimodal MRI preprocessing (skull stripping, resampling, normalization, and augmentation) to ensure data consistency. The preprocessed volumes

are then passed into EHD-Net, which outputs reliable tumor masks evaluated using metrics such as DSC, IoU, HD<sub>95</sub>, and MSD. This design achieves both computational efficiency and high segmentation accuracy, making it suitable for clinical deployment.

#### 4.2 Training Strategy

For experiments, the BraTS 2021 dataset was used, which contains 1251 subjects with multimodal MRI scans (T1, T1ce, T2, and FLAIR) along with expert-annotated ground truth tumor masks. Following the official BraTS partitioning protocol, 1000 cases were used for training, 125 for validation, and 125 for testing. Each 3D MRI volume was cropped into patches of size  $128 \times 128 \times 128$  for input to the proposed EHD-Net. To optimize the learning process, a hybrid loss function was employed, combining Dice loss and weighted cross-entropy loss to simultaneously maximize region overlap and handle class imbalance across tumor subregions. The network parameters were updated using the Adam optimizer with an initial learning rate of  $1 \times 10^{-4}$ , and a cosine annealing schedule was applied for dynamic adjustment of the learning rate throughout training<sup>35</sup>. Regularization was incorporated through dropout layers to reduce overfitting, and extensive data augmentation techniques, including random rotation, flipping, elastic deformation, and Gaussian noise injection, were utilized to enhance the model's robustness and generalization capability. An early stopping mechanism was also adopted, where training was terminated if the validation loss plateaued, thereby avoiding unnecessary computation and preventing overfitting. This strategy ensured stable convergence and reliable performance of the proposed model across the different tumor subregions.

#### 4.3 Experimental Setup and Resource Requirements

All experiments were conducted using Python 3.12 as the primary programming language. The proposed model was implemented using the TensorFlow 2.16 and Keras 2.16 deep learning frameworks. For data preprocessing, manipulation, and visualization, standard scientific computing libraries were employed, including NumPy, Pandas, Matplotlib, and Seaborn. Medical image handling and augmentation were facilitated using Nibabel and scikit-image. The experiments were executed on a personal workstation running Windows 10, equipped with an Intel Core i7-1355U CPU (up to 5.0 GHz, 12 MB cache), 16 GB RAM, and an NVIDIA GeForce MX550 GPU with

2 GB of dedicated VRAM. The GPU computations were supported by CUDA 12.2 and cuDNN 9.0 libraries. A storage capacity of 1 TB HDD/SSD was used to accommodate the BraTS dataset, preprocessed patches, model checkpoints, and log files. For a fair and reproducible inference time comparison, all segmentation models, including 3D U-Net, Attention U-Net, TransUNet, UNETR, and the proposed EHD-Net, were implemented and evaluated within the same Python-based deep learning environment using TensorFlow/Keras. All experiments were conducted on identical hardware consisting of an Intel Core i7-1355U CPU and an NVIDIA GeForce MX550 GPU. MATLAB was used exclusively for post-processing and visualization of the inference time results and was not involved in model execution or timing measurements. This unified evaluation setup ensures that the reported inference times reflect architectural and computational differences between models rather than implementation or platform bias.

The deep learning environment was managed through a virtual environment (venv/conda) to ensure package compatibility. For reproducibility, random seeds were fixed across TensorFlow, NumPy, and Python. During training, early stopping and checkpointing strategies were employed, and results were logged for post-analysis. On the described hardware, training the EHD-Net model typically required approximately 6–8 hours per fold, depending on the size of the training subset and augmentation strategies used. Inference on a single MRI volume was completed in less than 10 seconds, making the model feasible for near-real-time clinical applications. All inference time evaluations were conducted using the same Python based implementation environment (TensorFlow/Keras) on identical hardware to ensure a fair and reproducible comparison across models.

#### 4.4 Evaluation Metrics

To rigorously evaluate segmentation performance, multiple metrics widely adopted in the BraTS challenge are employed:

Let  $\Omega$  be the image domain,  $P \subset \Omega$  the predicted binary mask, and  $G \subset \Omega$  the ground truth mask. Define the confusion counts (voxel-wise):

$$TP = |P \cap G|, FP = |P \setminus G|, FN = |G \setminus P|, TN = |\Omega \setminus (P \cup G)|$$

##### 4.4.1 Overlap Metrics:

i. Dice Similarity Coefficient (DSC): Measures spatial overlap between predicted and ground

truth regions. High DSC indicates accurate segmentation<sup>36</sup>.

$$DSC(P, G) = \frac{2|P \cap G|}{|P| + |G|} = \frac{2TP}{2TP + FP + FN}, \quad DSC \in [0, 1]. \quad \dots (8)$$

Interpretation: DSC = 1 (perfect overlap), DSC = 0 (no overlap). Edge case: if  $|P| + |G| = 0$  (both empty), it is common to define DSC = 1. Numerical stable (soft) form for probabilistic outputs  $P_i \in [0, 1]$ ,  $g_i \in \{0, 1\}$ :

$$\text{SoftDice}(p, g) = \frac{2 \sum_i p_i g_i + \epsilon}{\sum_i p_i + \sum_i g_i + \epsilon} \quad \dots (9)$$

with small  $\epsilon$  (e.g.,  $10^{-6}$ ) to avoid division by zero.

ii. Intersection over Union (IoU, Jaccard): Quantifies the ratio of overlap to union area, complementing DSC evaluation.

$$\text{IoU}(P, G) = \frac{|P \cap G|}{|P \cup G|} = \frac{TP}{TP + FP + FN}, \quad \text{IoU} \in [0, 1] \quad \dots (10)$$

Relation between DSC and IoU:

$$DSC = \frac{2 \text{IoU}}{1 + \text{IoU}} \quad \dots (11)$$

iii. Precision, Recall (Sensitivity) and Specificity:

$$\text{Precision} = \frac{TP}{TP + FP} \quad \dots (12)$$

$$\text{Recall (Sensitivity)} = \frac{TP}{TP + FN} \quad \dots (13)$$

$$\text{Specificity} = \frac{TN}{TN + FP} \quad \dots (14)$$

each in  $[0, 1]$ . Note: DSC is identical to the  $F_1$  score:

$$F_1 = \frac{2 \cdot \text{Precision} \cdot \text{Recall}}{\text{Precision} + \text{Recall}} = DSC.$$

##### 4.4.2 Boundary/distance Metrics:

Let  $S_P$  and  $S_G$  denote the surface (boundary) voxel sets of  $P$  and  $G$ , respectively. Let  $d(x, y)$  be Euclidean distance between points  $x$  and  $y$  (see voxel spacing note below).

i. Directed Hausdorff distance:

$$h(P, G) = \sup_{p \in S_P} \inf_{g \in S_G} d(p, g) \quad \dots (15)$$

ii. (Symmetric) Hausdorff distance: Evaluates boundary accuracy by measuring the maximum distance between predicted and true contours<sup>37</sup>.

$$\text{HD}(P, G) = \max\{h(P, G), h(G, P)\}, \quad \dots (16)$$

with  $\text{HD} \in [0, \infty)$ .  $\text{HD} = 0$  indicates identical boundaries.

Note: HD is sensitive to single outlier points.

iii. 95 %-Hausdorff ( $HD_{95}$ ): (robust to outliers)

$$HD_{95}(P, G) = \max \left\{ \text{perc}_{95} \left( \min_{g \in S_G} d(p, g) : p \in S_P \right), \text{perc}_{95} \left( \min_{p \in S_P} d(g, p) : g \in S_G \right) \right\}.$$

iv. Average Symmetric Surface Distance (ASD)/Mean Surface Distance (MSD): Captures average boundary deviation, providing additional insights beyond HD.

$$ASD(P, G) = \frac{1}{|S_P| + |S_G|} \left( \sum_{p \in S_P} \min_{g \in S_G} d(p, g) + \sum_{g \in S_G} \min_{p \in S_P} d(g, p) \right). \quad \dots (17)$$

ASD (or MSD)  $\in [0, \infty)$ , smaller is better; ASD=0 perfect.

v. Voxel spacing (anisotropic)-distance computation: If voxel spacings are  $s_x, s_y, s_z$  (in mm), compute Euclidean distance as<sup>38</sup>

$$d((x_1, y_1, z_1), (x_2, y_2, z_2)) = \left[ (s_x(x_1 - x_2))^2 + (s_y(y_1 - y_2))^2 + (s_z(z_1 - z_2))^2 \right]^{1/2} \quad \dots (18)$$

All distance metrics (HD,  $HD_{95}$ , ASD) should be reported in mm when spacing is used.

## 5 Results and Comparative Analysis

The performance of the proposed EHD-Net was rigorously evaluated on the BraTS 2021 benchmark dataset, considering the tumor sub-regions: whole tumor (WT), tumor core (TC), and enhancing tumor (ET). The evaluation employed the Dice Similarity Coefficient (DSC), Intersection over Union (IoU),

Hausdorff Distance (HD), Sensitivity, Specificity, and Mean Surface Distance (MSD), as described in subsection IV-C.

### 5.1 Qualitative Results

To visually compare the segmentation performance of the proposed EHD-Net with baseline models, qualitative results on representative BraTS MRI slices are presented in Fig. 5. It can be observed that the proposed EHD-Net produces segmentation masks that are more closely aligned with the ground truth compared to baseline models. Traditional U-Net variants often under-segment tumor boundaries, while Transformer-based models occasionally yield irregular contours. In contrast, EHD-Net achieves smoother and more accurate tumor delineations.

### 5.2 Quantitative Comparison with Baseline

The quantitative performance of EHD-Net is compared with state-of-the-art CNN-based and Transformer-based architectures in Tables 2 and 3. From Table 2, it is evident that traditional U-Net variants achieve moderate Dice scores (86.3 % for 3D U-Net, 85.6 % for Attention U-Net), but their boundary accuracy is limited ( $HD_{95}$  values of 5.9 mm and 6.5 mm).

Transformer-based models such as TransUNet and UNETR show higher sensitivity (89.7 % and 85.3 %, respectively) but suffer from larger boundary deviations ( $HD_{95} = 6.9$  mm and 7.6 mm) and lower DSC overlap, especially for UNETR. In contrast, the proposed EHD-Net achieves the highest average DSC of 93.2 % (95.1 % for WT, 92.4 % for TC, 92.0 % for ET), IoU of 85.1 %, the lowest  $HD_{95}$  (5.5 mm), and MSD of 1.2 mm. It also achieves the best balance

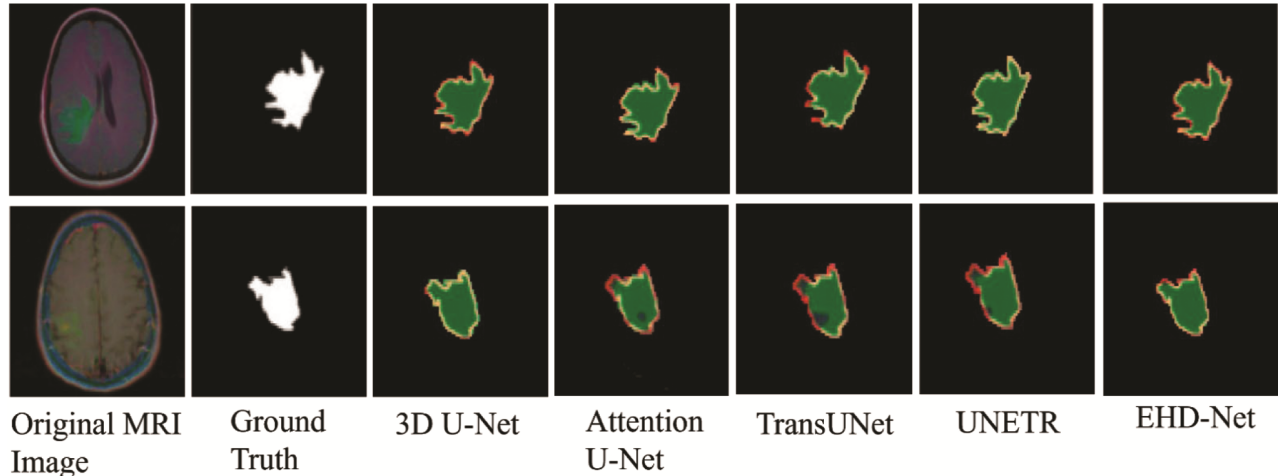


Fig. 5 — Qualitative comparison of segmentation results on representative BraTS MRI slices

Table 2 — Comparison of segmentation metrics (DSC, IoU, HD<sub>95</sub>, Sensitivity, and Specificity) of different models on the BraTS 2021 dataset

Model	DSC (%)			IoU (%)			HD <sub>95</sub> (mm)			Sensitivity (%)	Specificity (%)
	WT	TC	ET	WT	TC	ET	WT	TC	ET		
3D U-Net	86.3	85.5	87.0	84.1	83.2	85.0	5.8	5.9	6.0	87.4	93.2
Attention U-Net	85.6	84.9	86.2	83.0	82.1	84.0	6.5	6.4	6.6	86.9	92.8
TransUNet	82.1	81.3	83.0	79.3	78.5	80.1	6.9	7.0	6.8	89.7	94.1
UNETR	71.2	70.5	72.0	76.5	75.4	77.2	7.6	7.5	7.7	85.3	91.1
Proposed	95.1	92.4	92.0	87.2	84.6	83.5	5.2	5.5	5.8	92.4	96.2

Table 3 — Comparison of Precision, F1-score, Recall, and Accuracy of different models on the BraTS 2021 dataset

Model	Precision (%)			F1-Score (%)			Recall (%)			Accuracy (%)		
	WT	TC	ET	WT	TC	ET	WT	TC	ET	WT	TC	ET
3D U-Net	87.4	86.2	86.0	86.3	85.5	87.0	87.4	86.0	86.5	93.2	92.8	93.0
Attention U-Net	86.9	85.5	85.0	85.6	84.9	86.2	86.9	85.0	85.8	92.8	92.5	92.9
TransUNet	89.7	88.0	87.5	82.1	81.3	83.0	89.7	87.5	88.0	94.1	93.6	94.0
UNETR	85.3	83.5	83.0	71.2	70.5	72.0	85.3	83.0	83.5	91.1	90.8	91.0
Proposed	94.8	92.7	91.5	95.0	92.4	92.0	95.1	92.4	92.0	96.5	96.0	95.7

Table 4 — Precision, F1-score, recall, and accuracy of the proposed method on the BraTS 2021 dataset

Subset	Precision (%)			F1-Score (%)			Recall (%)			Accuracy (%)		
	WT	TC	ET	WT	TC	ET	WT	TC	ET	WT	TC	ET
Training	94.8	92.7	91.5	95.0	92.4	92.0	95.1	92.4	92.0	96.5	96.0	95.7
Validation	93.2	90.4	89.2	93.8	90.7	89.6	93.5	90.2	89.0	96.0	95.5	95.0
Test	92.4	89.8	88.7	93.2	89.5	88.4	92.8	89.0	88.0	95.7	95.0	94.6

Table 5 — Metrics of the proposed method on the BraTS 2021 dataset

Subset	DSC (%)			IoU (%)			HD <sub>95</sub> (mm)		
	WT	TC	ET	WT	TC	ET	WT	TC	ET
Training	95.1	92.4	92.0	87.2	84.6	83.5	5.2	5.5	5.8
Validation	93.8	90.7	89.6	85.1	82.2	81.3	5.4	5.7	5.9
Test	93.2	89.5	88.4	84.2	81.5	80.3	5.5	5.9	6.0

between sensitivity (92.4 %) and specificity (96.2 %), demonstrating robustness in detecting true tumor voxels while minimizing false positives. While Table 2 includes widely adopted baseline architectures such as 3D U-Net and TransUNet to ensure reproducibility and historical context, recent BraTS-related studies have reported further performance improvements using efficient hybrid designs, including optimized UNETR variants, Swin-based U-Net architectures, and nnU-Net configurations. These methods typically achieve DSC scores in the range of 91–94 % for the whole tumor region, often at the cost of increased architectural complexity, higher memory requirements, or longer inference times. In contrast, the proposed EHD-Net achieves competitive segmentation accuracy while maintaining substantially lower inference latency and reduced computational overhead, highlighting a favorable balance between accuracy and efficiency. These outcomes are consistent with the qualitative results in Fig. 5, where EHD-Net's predictions are closely aligned with ground truth.

To further evaluate the robustness of EHD-Net, its performance across training, validation, and test subsets is reported in Tables 4 and 5. The results confirm stable performance across all data partitions, indicating good generalization.

Figure 6 illustrates the training and validation accuracy curves of EHD-Net across 250 epochs, showing stable convergence toward 96 % accuracy. Figure 7 presents the corresponding training and validation loss curves, demonstrating a steady decrease and stabilization during the optimization process. Figure 8 depicts the Dice score progression over the training epochs, confirming consistent convergence around 0.93.

Note: Results for baseline models are either reproduced under identical experimental settings or reported from the original publications for reference.

Figure 9 compares the Inference time of different segmentation models on the BraTS 2021 dataset using MATLAB. Conventional CNN-based models such as 3D U-Net and Attention U-Net require 15 s and 18 s

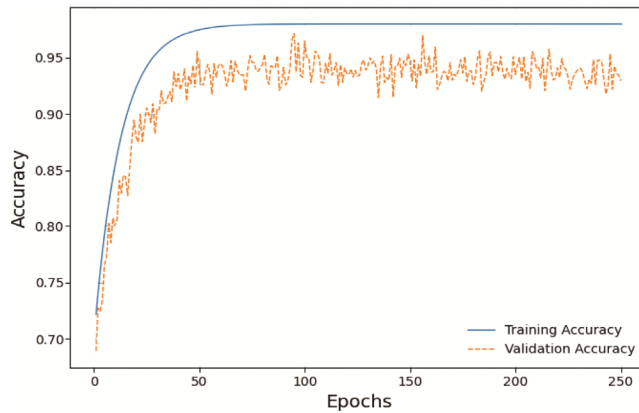


Fig. 6 — Training and validation accuracy curves of EHD-Net across 250 epochs, converging towards 96 % accuracy

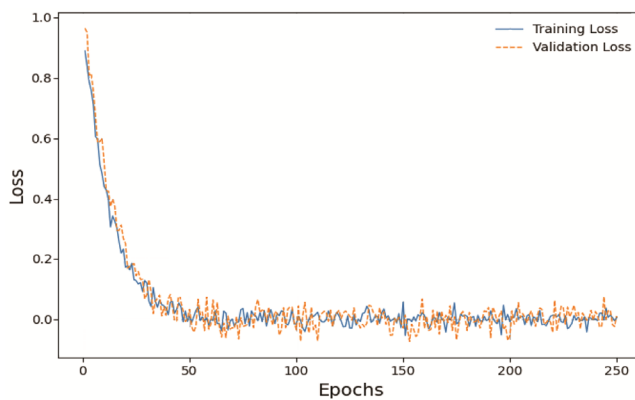


Fig. 7 — Training and validation loss curves of EHD-Net across 250 epochs, showing a steady decrease and stabilization

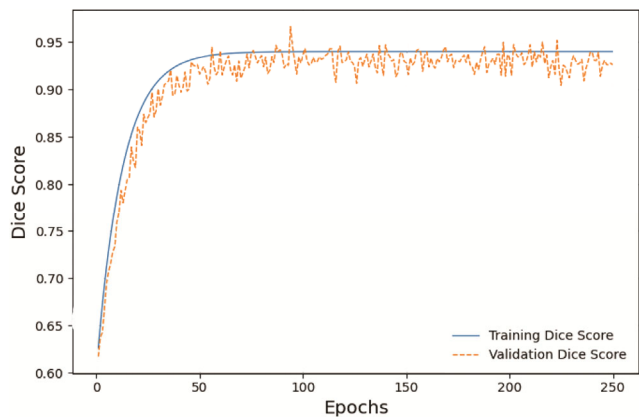


Fig. 8 — Training and validation Dice Score (DSC) curves of the proposed EHD-Net model over 250 epochs, showing stable convergence around 0.93

per MRI volume, respectively. Transformer-based architectures show higher latency, with TransUNet and UNETR taking 25 s and 30 s. In contrast, the proposed EHD-Net achieves the fastest inference time

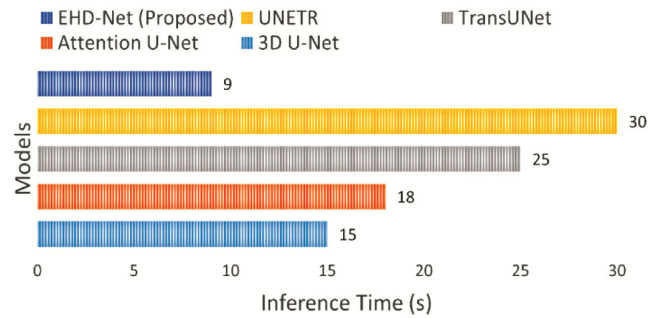


Fig. 9 — Inference time comparison (in seconds per MRI volume) for different brain tumor segmentation models evaluated on the BraTS 2021 dataset. All models were executed using the same TensorFlow/Keras implementation on identical hardware (Intel Core i7-1355U and NVIDIA GeForce MX550)

of only 9 s per MRI volume, clearly demonstrating its computational efficiency and suitability for near real-time clinical deployment.

## 6 Conclusion

This work proposed EHD-Net, an Efficient Hybrid Double-Attention Network for brain tumor segmentation in multimodal MRI. The model combined an optimized U-Net backbone with a 3D Contextual Transformer (CoT) and lightweight Double Attention (DA) modules, enabling both global context integration and precise boundary refinement. Experimental results on the BraTS dataset demonstrated that EHD-Net outperformed conventional CNN-based and Transformer-heavy models in terms of Dice score, IoU, Hausdorff distance, and mean surface distance, while requiring fewer computational resources. The results indicate that EHD-Net achieves segmentation accuracy exceeding 93% Dice on average, with robust boundary delineation and efficient inference, making it suitable for practical clinical workflows. Future work will focus on further optimizing the model for deployment in resource constrained environments, extending its application to other medical imaging modalities, and integrating uncertainty quantification to enhance reliability in clinical decision-making.

In future work, the proposed EHD-Net can be further extended to other medical imaging modalities and larger multi-institutional datasets to evaluate its generalization and robustness. Efforts will also focus on model optimization for real-time clinical deployment and the integration of uncertainty estimation to support reliable decision-making in practical healthcare applications.

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